

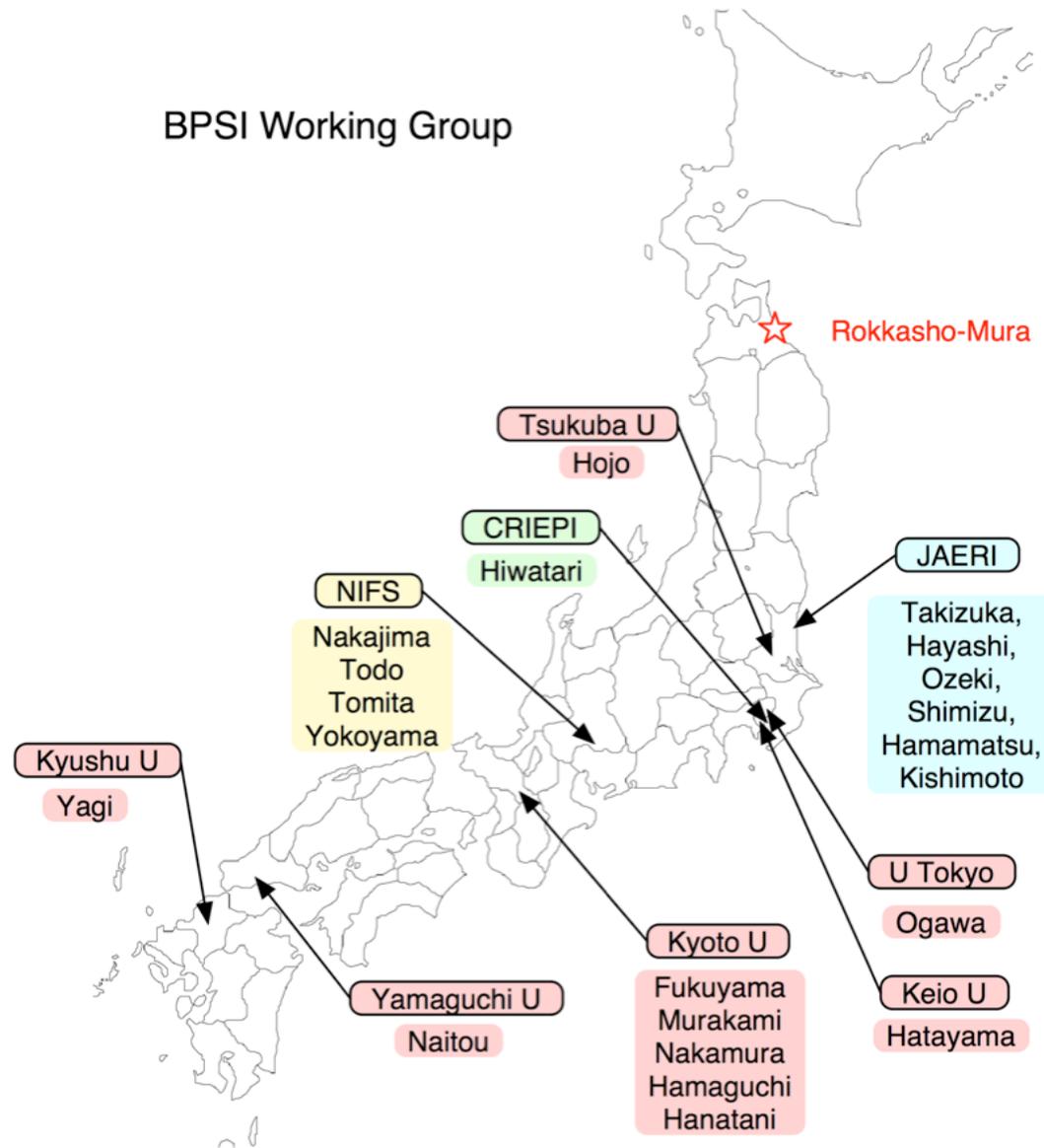
# Integrated Code Development for Burning Plasma Simulation

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M. Yagi (Kyushu U)

- Burning Plasma Simulation Initiative
- Integrate Code TASK
- Transport Analysis TASK/TR
- Preliminary ITER Plasma Simulation
- Transport Analysis TASK/TX

# Burning Plasma Simulation Initiative

## Collaboration of Universities, NIFS and JAERI



# Activities of BPSI

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## Framework of Integrated Code:

- Standard interface for data transfer
- Reference core code: **TASK**

## Modeling of Phenomena with Different Scales:

- Transport-MHD hierarchical model
- Core-SOL interface model
- Transport modeling in the presence of islands

## Advanced Computational Technique:

- Parallel processing
- Distributed computing
- Visualization

# TASK code

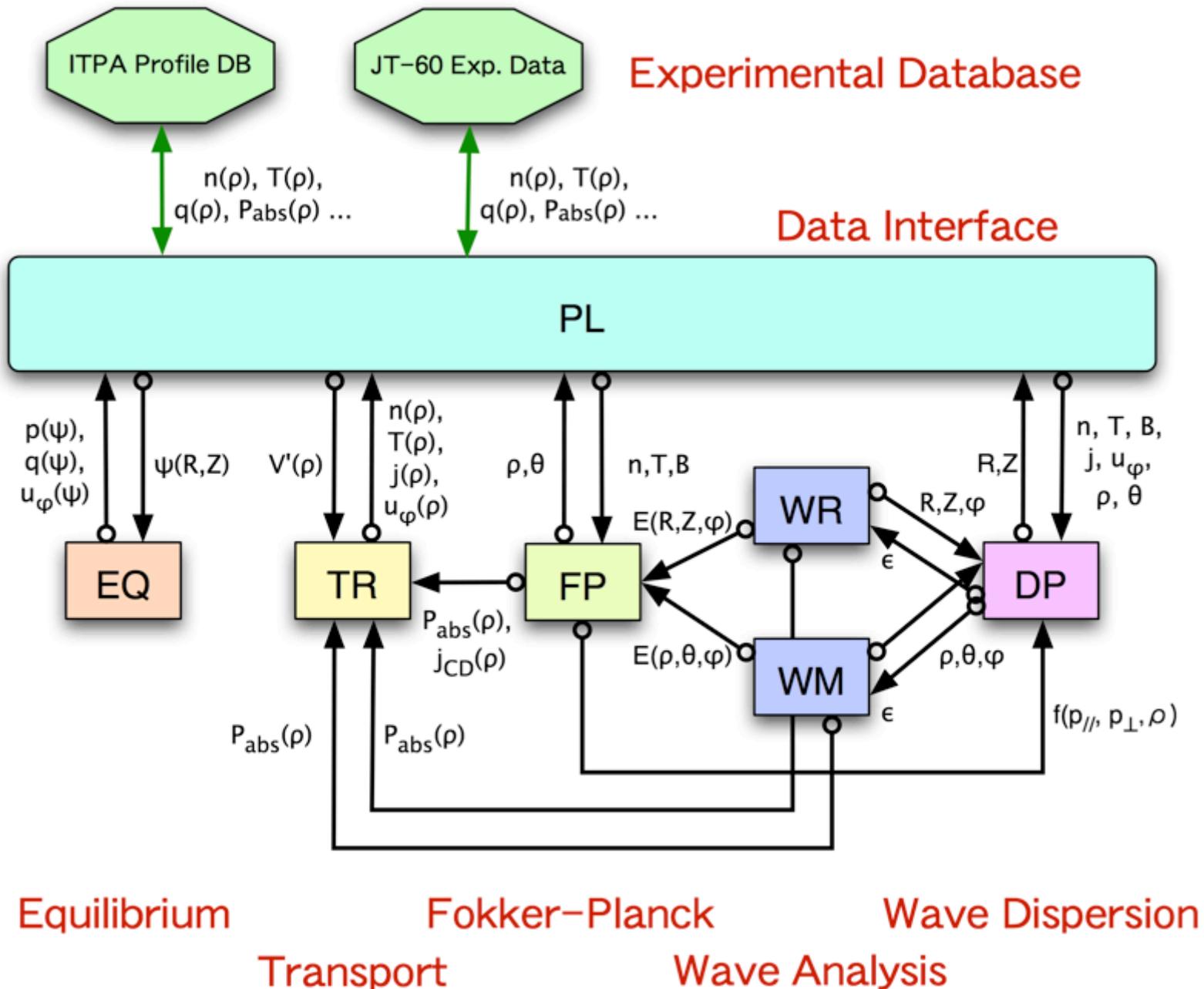
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- Transport Analyzing System for Tokamak
- Modules

TASK/EQ	2D Equilibrium	Fixed boundary
TR	1D Transport	Diffusive model
TX	1D Transport	Dynamical model
FP	3D Fokker-Planck	Bounce averaged
WR	Ray/Beam Tracing	EC, LH
WM	Full Wave	IC,AE
DP	Wave Dispersion	Various models
LIB	Common Library	
PL	Data Conversion	Profile database

- Features:  
modular structure, various H&CD scheme, high portability,  
development using CVS, extension for helical plasmas

# Structure of TASK Code



# ECED analysis : TASK/WR/FP/DP

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- **Geometrical Optics: TASK/WR**

- **Ray Tracing Method:**

- Plane wave: beam size  $d \gg \lambda$  wave length

- **Beam Tracing Method**

- Analysis of wave propagation with finite beam size

- **Beam shape** : Gaussian beam

$$E(\mathbf{r}) = \text{Re} [C(\mathbf{r}) \mathbf{e}(\mathbf{r}) e^{i s(\mathbf{r}) - \phi(\mathbf{r})}]$$

- $C$ : amplitude,  $\mathbf{e}$ : polarization,  $s(\mathbf{r}) + i \phi(\mathbf{r})$ : phase

$$s(\mathbf{r}) = s_0(\tau) + k_\alpha^0(\tau)[r^\alpha - r_0^\alpha(\tau)] + \frac{1}{2}s_{\alpha\beta}[r^\alpha - r_0^\alpha(\tau)][r^\beta - r_0^\beta(\tau)]$$

$$\phi(\tau) = \frac{1}{2}\phi_{\alpha\beta}[r^\alpha - r_0^\alpha(\tau)][r^\beta - r_0^\beta(\tau)]$$

- $r_0$ : position of beam axis,  $k^0$ : wave number on beam axis

- **Curvature radius**:  $R_\alpha = 1/\lambda s_{\alpha\alpha}$ , **Beam radius**:  $d_\alpha = \sqrt{2/\phi_{\alpha\alpha}}$

- **18 Ordinally Differential Equations** for  $r_\alpha$ ,  $k_\alpha$ ,  $s_{\alpha\beta}$  and  $\phi_{\alpha\beta}$ ,

# Fokker-Planck Analysis : TASK/FP

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- **Fokker-Planck equation** for **velocity distribution function**  $f(p_{\parallel}, p_{\perp}, \psi, t)$

$$\frac{\partial f}{\partial t} = E(f) + C(f) + Q(f) + L(f)$$

- $E(f)$ : Acceleration term due to DC electric field
  - $C(f)$ : Coulomb collision term
  - $Q(f)$ : Quasi-linear term due to wave-particle resonance
  - $L(f)$ : Spatial diffusion term
- **Bounce-averaged**: Trapped particle effect, zero banana width
  - **Relativistic**: momentum  $p$ , weakly relativistic collision term
  - **Nonlinear collision**: momentum conservation, energy conservation
  - **Three-dimensional**: spatial diffusion (classical, neoclassical, turbulence)

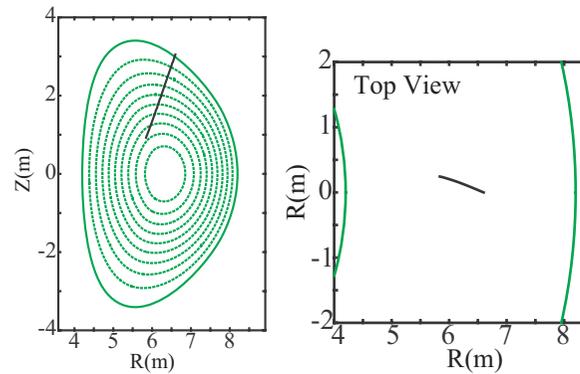
# Wave Dispersion Analysis : TASK/DP

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- **Various Models of Dispersion Tensor  $\overset{\leftrightarrow}{\epsilon}(\omega, k; r)$ :**
  - **Resistive MHD model**
  - **Collisional cold plasma model**
  - **Collisional warm plasma model**
  - **Kinetic plasma model (Maxwellian, non-relativistic)**
  - **Kinetic plasma model (Arbitrary  $f(v)$ , non-relativistic)**
  - **Kinetic plasma model (Arbitrary  $f(v)$ , relativistic)**
  - **Gyro-kinetic plasma model (Maxwellian, non-relativistic)**
  - **Gyro-kinetic plasma model (Arbitrary  $f(v)$ , non-relativistic)**
- **Arbitrary  $f(v)$ :**
  - **Relativistic Maxwellian**
  - **Output of TASK/FP**

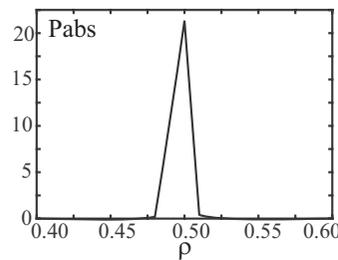
# Analysis of ECCD by TASK Code

Poloidal angle  $70^\circ$   
 Toroidal angle  $20^\circ$   
 Initial beam radius  $0.05 \text{ m}$   
 Initial beam curvature  $2 \text{ m}$

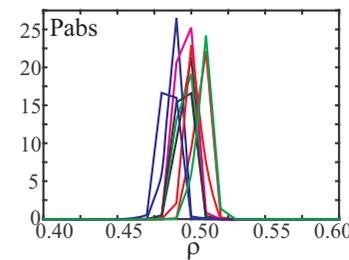


Ray/Beam Profile

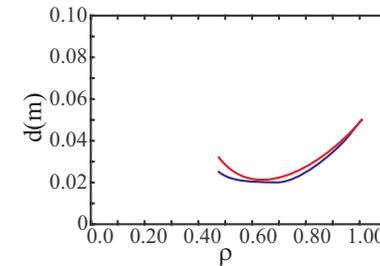
One Ray



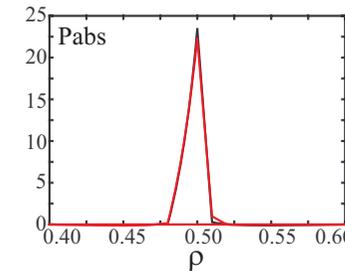
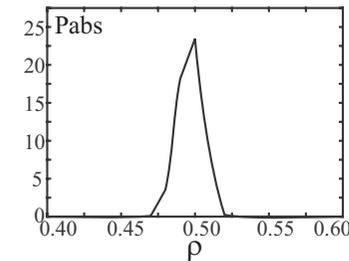
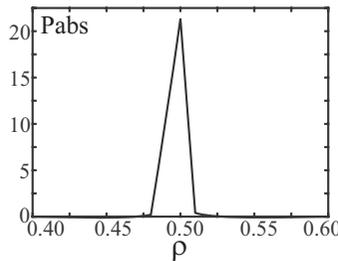
Multi Rays



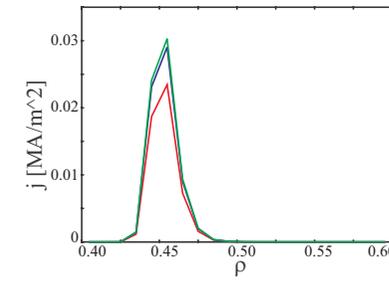
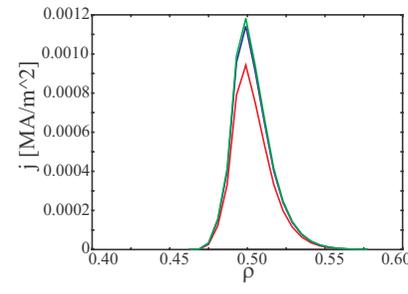
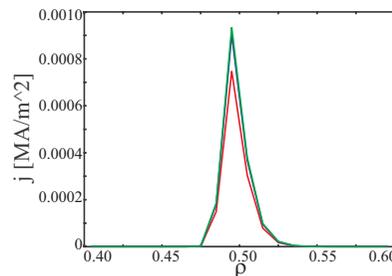
Beam Tracing



$P_{abs}$  Profile



$j_{CD}$  Profile



# Full wave analysis: TASK/WM

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- **magnetic surface coordinate:**  $(\psi, \theta, \varphi)$

- Boundary-value problem of **Maxwell's equation**

$$\nabla \times \nabla \times \mathbf{E} = \frac{\omega^2}{c^2} \overset{\leftrightarrow}{\epsilon} \cdot \mathbf{E} + i \omega \mu_0 \mathbf{j}_{\text{ext}}$$

- Kinetic **dielectric tensor:**  $\overset{\leftrightarrow}{\epsilon}$

- **Wave-particle resonance:**  $Z[(\omega - n\omega_c)/k_{\parallel}v_{\text{th}}]$
- **Fast ion: Drift-kinetic**

$$\left[ \frac{\partial}{\partial t} + v_{\parallel} \nabla_{\parallel} + (\mathbf{v}_d + \mathbf{v}_E) \cdot \nabla + \frac{e_{\alpha}}{m_{\alpha}} (v_{\parallel} E_{\parallel} + \mathbf{v}_d \cdot \mathbf{E}) \frac{\partial}{\partial \varepsilon} \right] f_{\alpha} = 0$$

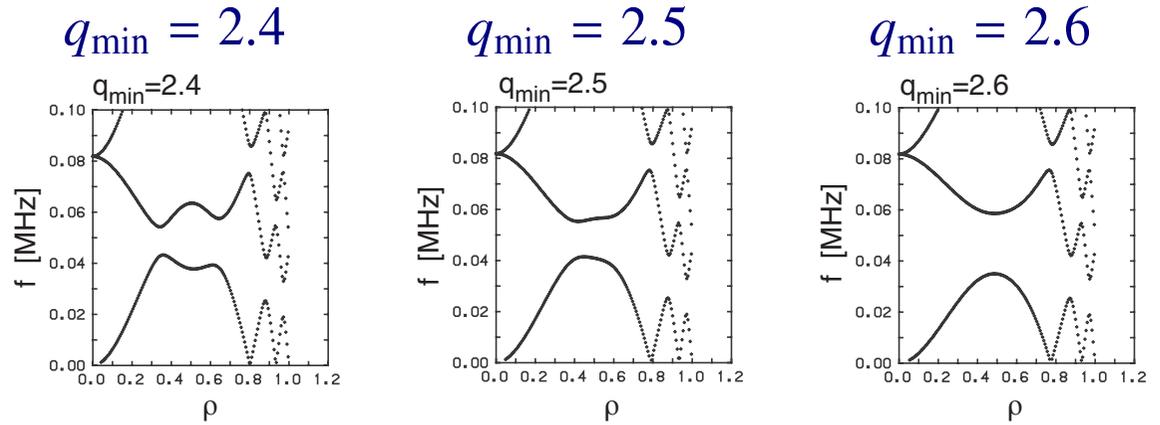
- Poloidal and toroidal **mode expansion**

- **Accurate estimation of  $k_{\parallel}$**

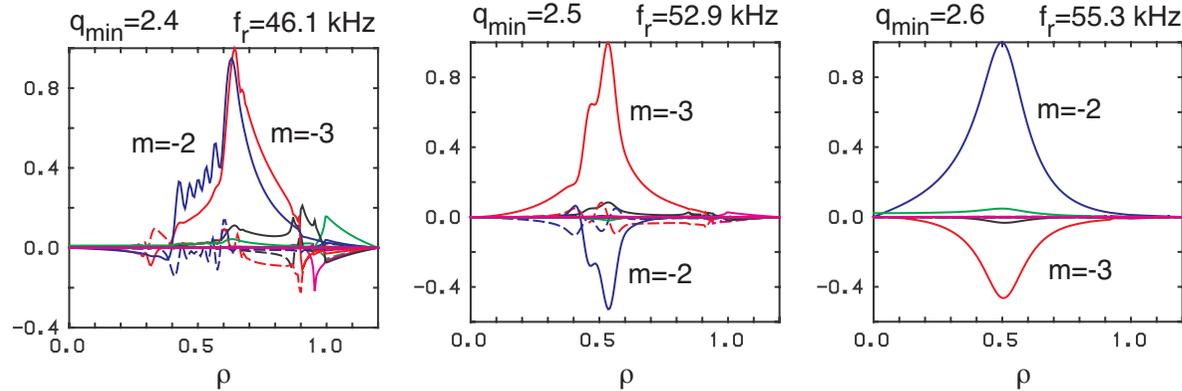
- Eigenmode analysis: **Complex eigen frequency** which maximize wave amplitude for fixed excitation proportional to electron density

# Eigenmode Structure in Reversed Shear Configuration

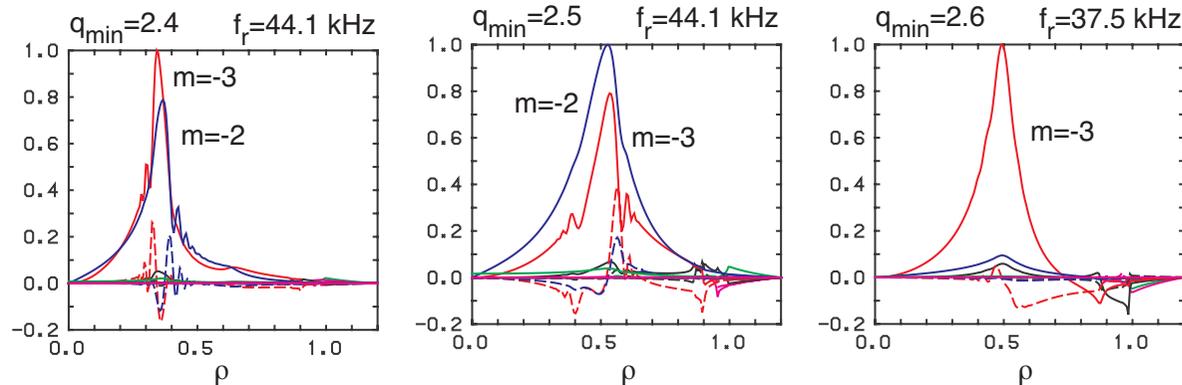
Alfvén resonance



Higher freq.



Lower freq.



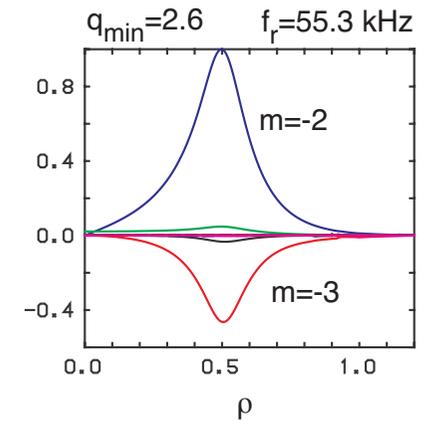
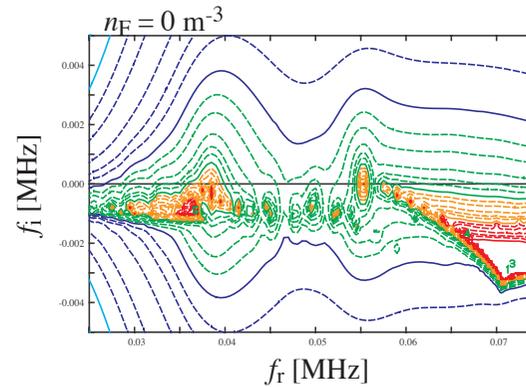
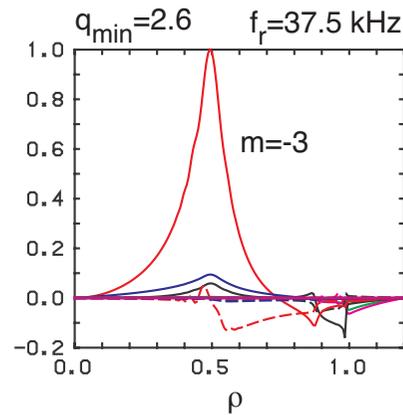
TAEs

Double TAE

RSAE

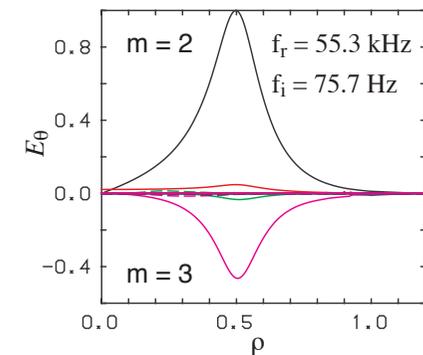
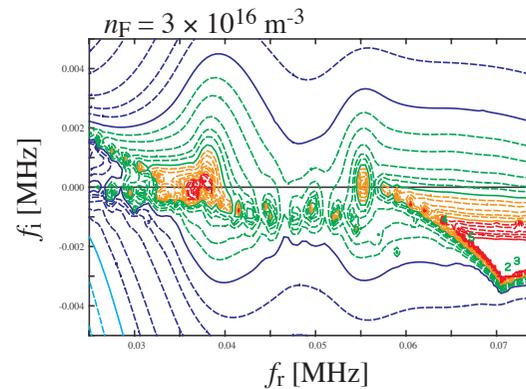
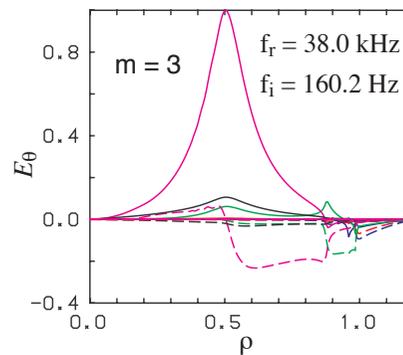
# Excitation by Energetic Particles ( $q_{\min} = 2.6$ )

- Without EP



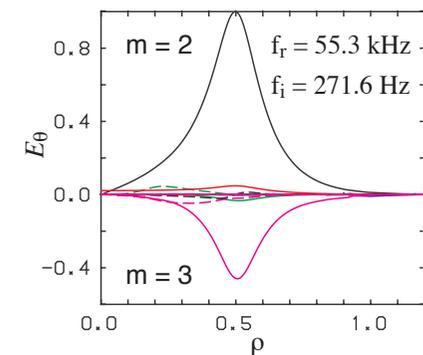
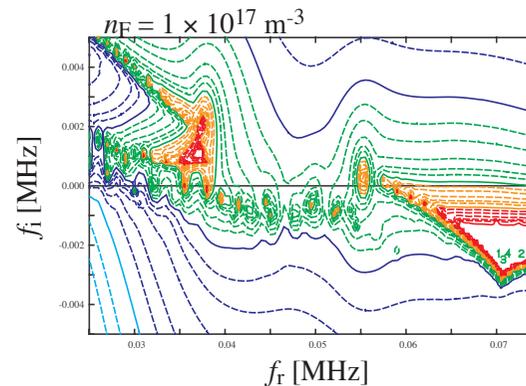
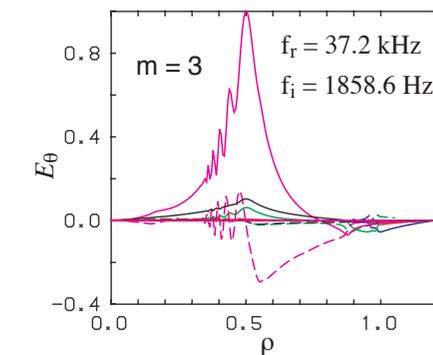
- With EP

$3 \times 10^{16}$  m<sup>-3</sup>  
 360 keV  
 0.5 m



- With EP

$1 \times 10^{17}$  m<sup>-3</sup>  
 360 keV  
 0.5 m



# Transport Analysis

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- **Level of Analysis:**

- **TASK/TR:** Diffusive transport equation: Flux-Gradient relation
- **TASK/TX:** Dynamical transport equation: Flux-averaged fluid equation (plasma rotation, transient phenomena)
- **TASK/FP:** Kinetic transport equation: Bounce-averaged Fokker-Plank equation

- **Diffusive transport equation:**  $V$ : Volume,  $\rho$ : Normalized radius,  $V' = dV/d\rho$

- **Particle transport**

$$\frac{1}{V'} \frac{\partial}{\partial t} (n_s V') = - \frac{\partial}{\partial \rho} \left( \langle |\nabla \rho| \rangle n_s V_s - \langle |\nabla \rho|^2 \rangle D_s \frac{\partial n_s}{\partial \rho} \right) + S_s$$

- **Heat transport**

$$\frac{1}{V'^{5/3}} \frac{\partial}{\partial t} \left( \frac{3}{2} n_s T_s V'^{5/3} \right) = - \frac{1}{V'} \frac{\partial}{\partial \rho} \left( V' \langle |\nabla \rho| \rangle \frac{3}{2} n_s T_s V_{Es} - V' \langle |\nabla \rho|^2 \rangle n_s \chi_s \frac{\partial T_s}{\partial \rho} \right) + P_s$$

- **Current diffusion**

$$\frac{\partial B_\theta}{\partial t} = \frac{\partial}{\partial \rho} \left[ \frac{\eta}{FR_0 \langle R^{-2} \rangle \mu_0} \frac{R_0 F^2}{V'} \frac{\partial}{\partial \rho} \left( \frac{V' B_\theta}{F} \left\langle \frac{|\nabla \rho|^2}{R^2} \right\rangle \right) - \frac{\eta}{FR_0 \langle R^{-2} \rangle} \langle \mathbf{J} \cdot \mathbf{B} \rangle_{\text{ext}} \right]$$

# Diffusive Transport Analysis: TASK/TR

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- **Transport Equation Based on Gradient-Flux Relation**
  - **Multi thermal species**: e.g. Electron, D, T, He
    - Density, thermal energy, (toroidal rotation)
  - **Two beam components**: Beam ion, Energetic  $\alpha$ 
    - Density, toroidal rotation
  - **Neutral**: Two component (cold and hot), Diffusion equation
  - **Impurity**: Thermal species or fixed profile
- **Transport Model**
  - **Neoclassical**: Wilson, Hinton & Hazeltine, Sauter, NCLASS
  - **Turbulent**: CDBM (current diffusive ballooning mode), GLF23 (V1.61)
- **Sources**
  - Heating and current data: Interface to TASK/WR/WM/FP, Analytical
  - Simple NBI, Nuclear fusion, Ionization, Charge exchange, Radiation
- **Interface to Experimental Data**
  - UFILE

# CDBM Turbulence Model

- **Marginal Stability Condition** ( $\gamma = 0$ )

$$\chi_{\text{TB}} = F(s, \alpha, \kappa, \omega_{E1}) \alpha^{3/2} \frac{c^2}{\omega_{pe}^2} \frac{v_A}{qR}$$

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**Magnetic shear**  $s \equiv \frac{r}{q} \frac{dq}{dr}$

**Pressure gradient**  $\alpha \equiv -q^2 R \frac{d\beta}{dr}$

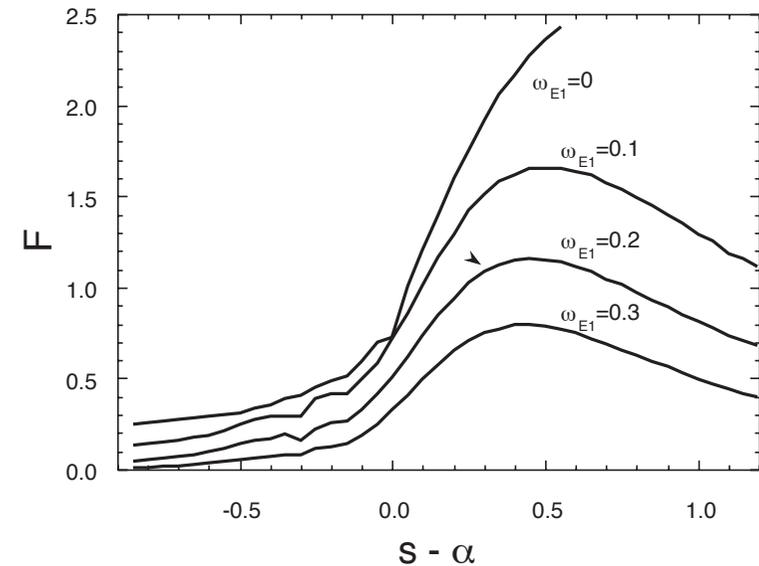
**Magnetic curvature**  $\kappa \equiv -\frac{r}{R} \left(1 - \frac{1}{q^2}\right)$

**$E \times B$  rotation shear**  $\omega_{E1} \equiv \frac{r^2}{sv_A} \frac{d}{dr} \frac{E}{rB}$

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- **Weak and negative magnetic shear, Shafranov shift and  $E \times B$  rotation shear**  
**reduce thermal diffusivity.**

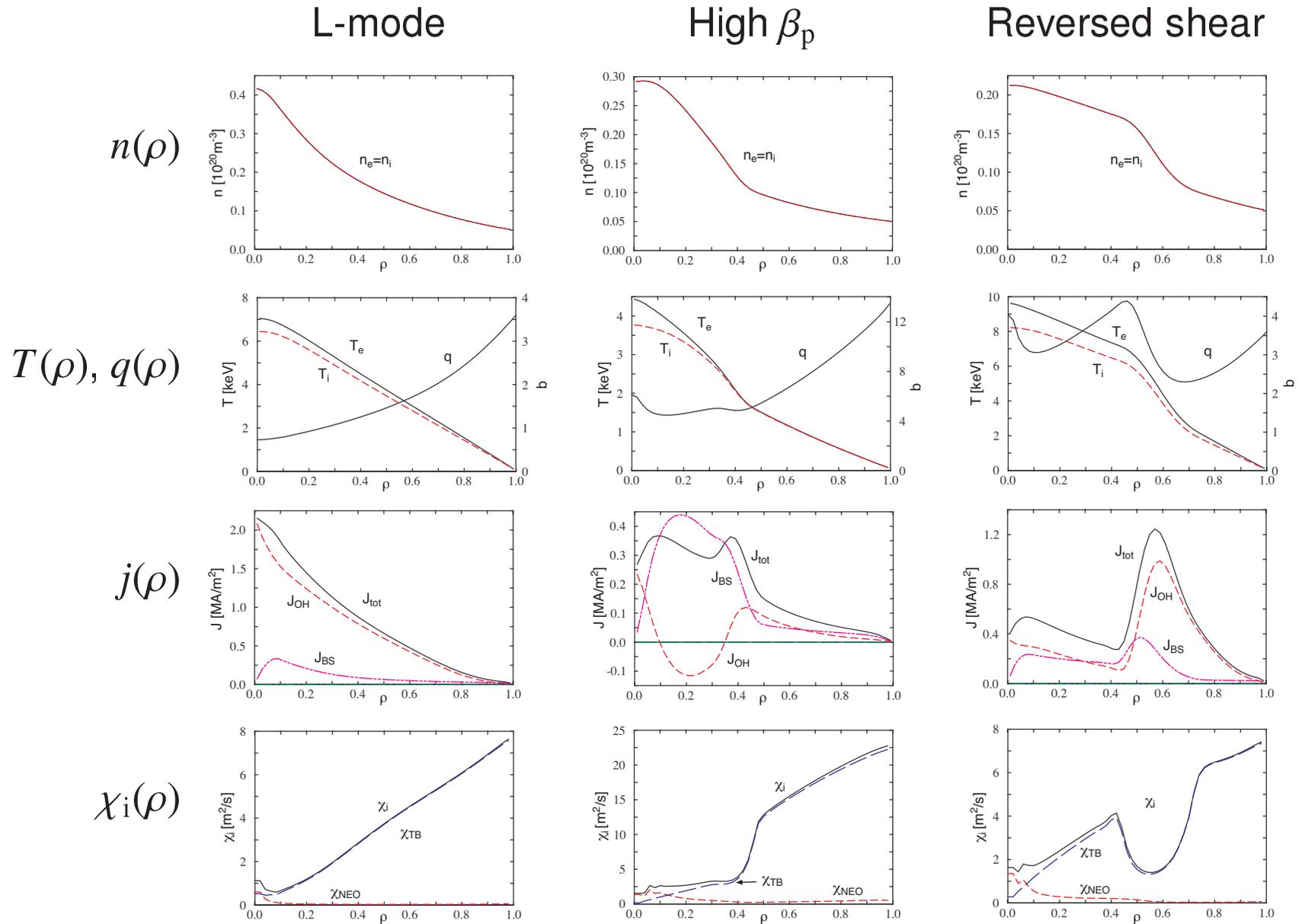
$s - \alpha$  dependence of  $F(s, \alpha, \kappa, \omega_{E1})$



## Fitting Formula

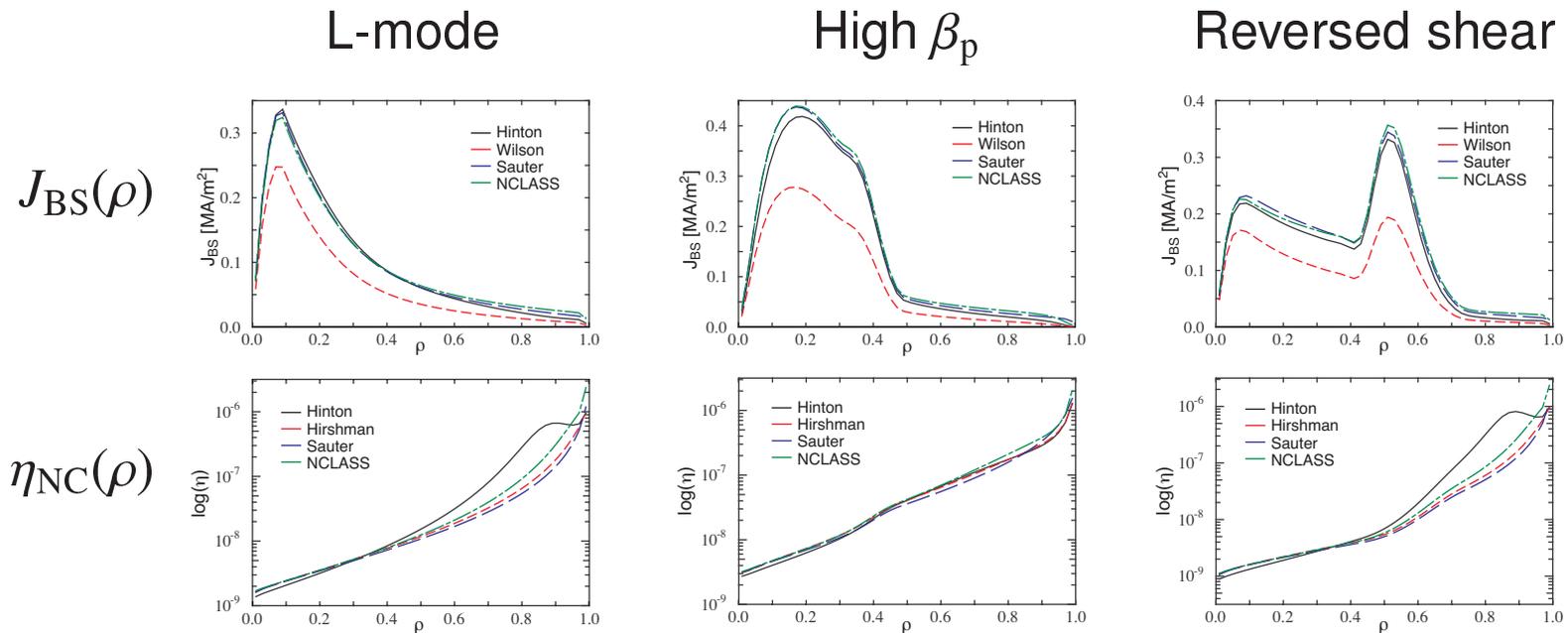
$$F = \begin{cases} \frac{1}{1 + G_1 \omega_{E1}^2} \frac{1}{\sqrt{2(1 - 2s')(1 - 2s' + 3s'^2)}} & \text{for } s' = s - \alpha < 0 \\ \frac{1}{1 + G_1 \omega_{E1}^2} \frac{1 + 9\sqrt{2}s'^{5/2}}{\sqrt{2}(1 - 2s' + 3s'^2 + 2s'^3)} & \text{for } s' = s - \alpha > 0 \end{cases}$$

# Typical Profile



# Neoclassical Transport Model

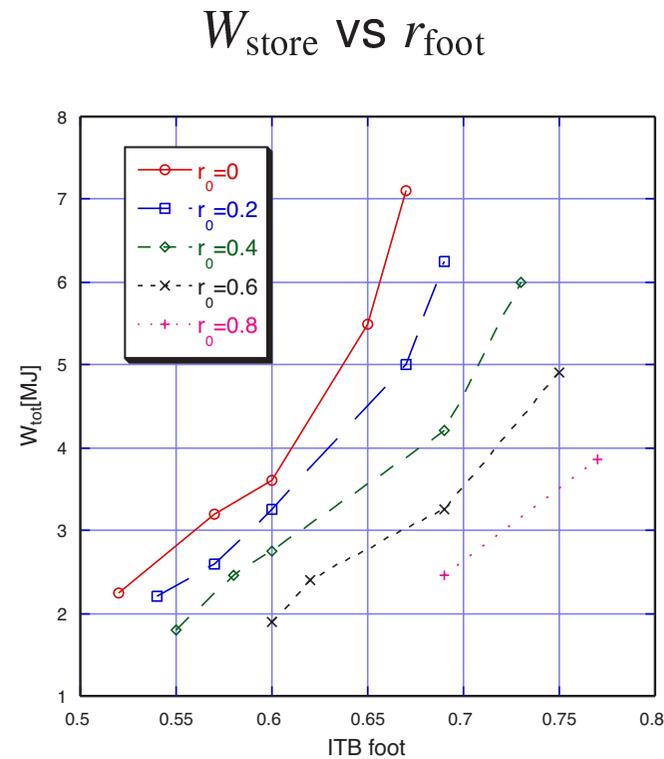
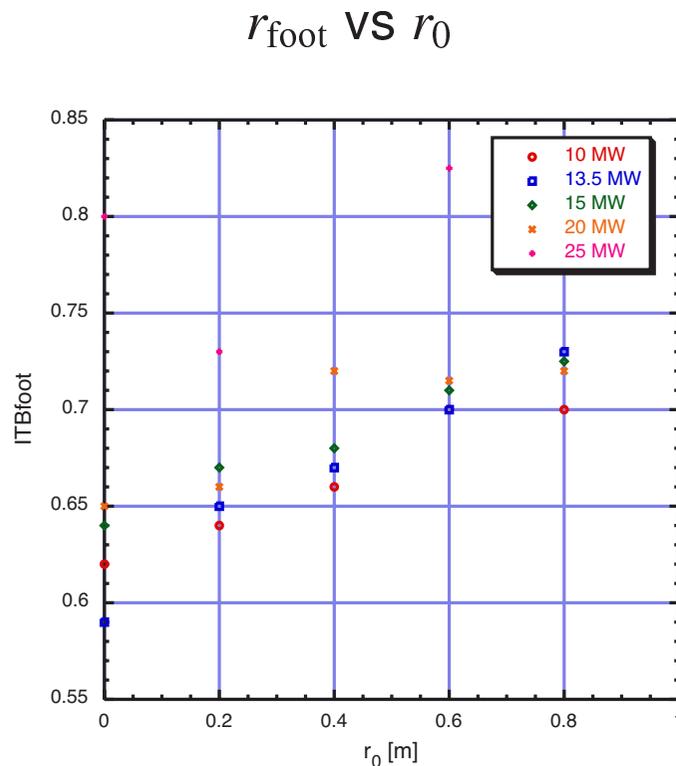
- **Comparison of Bootstrap Current and Resistivity**
  - **Wilson model**: from “Tokamaks 2nd ed” (Wesson)
  - **Hinton and Hazeltine model**
  - **Sauter model**
  - **NCLASS package** (Houlberg)



- **Fairly good agreement except Wilson model**

# ITB Foot Location and Store Energy

- **High  $\beta_p$  mode**
- Heating center radius  $r_0$  and heating power  $P_H$  are changed.
- **ITB foot location  $r_{\text{foot}}$ , Stored energy  $W_{\text{store}}$**



- **With the increase of  $P_H$ ,  $r_{\text{foot}}$  and  $W_{\text{store}}$  increases.**
- **If  $P_H$  fixed,  $W_{\text{store}}$  decreases with the increase of  $r_0$ .**

# Comparison with JT-60 Experiment

- **Reversed Shear Configuration**

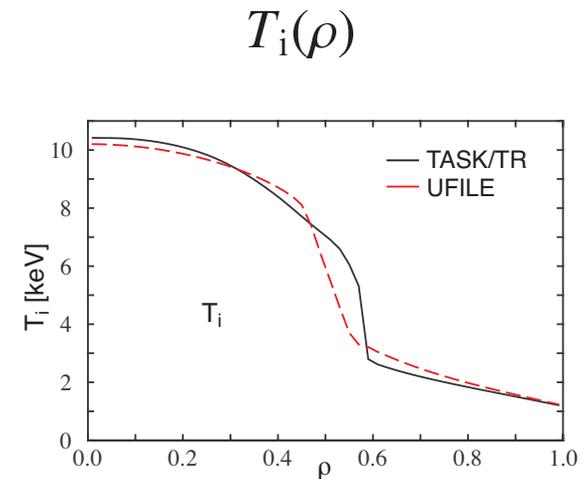
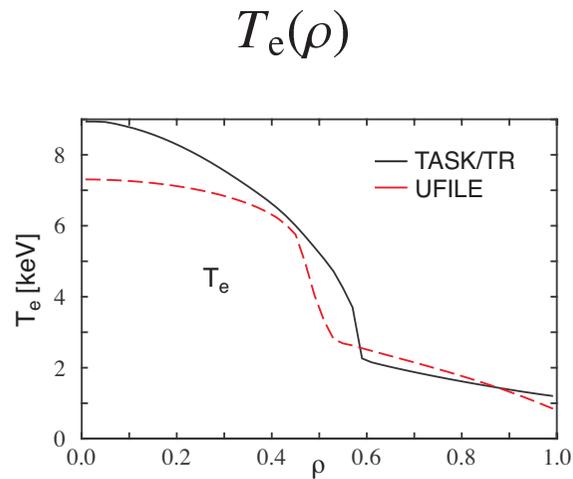
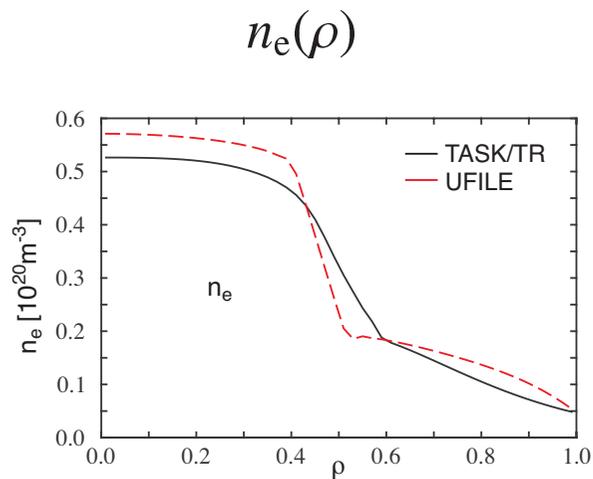
- **Shot number: 29728**

- Profiles  $q$ ,  $P_e$ ,  $P_i$ : given

- Metric data: given

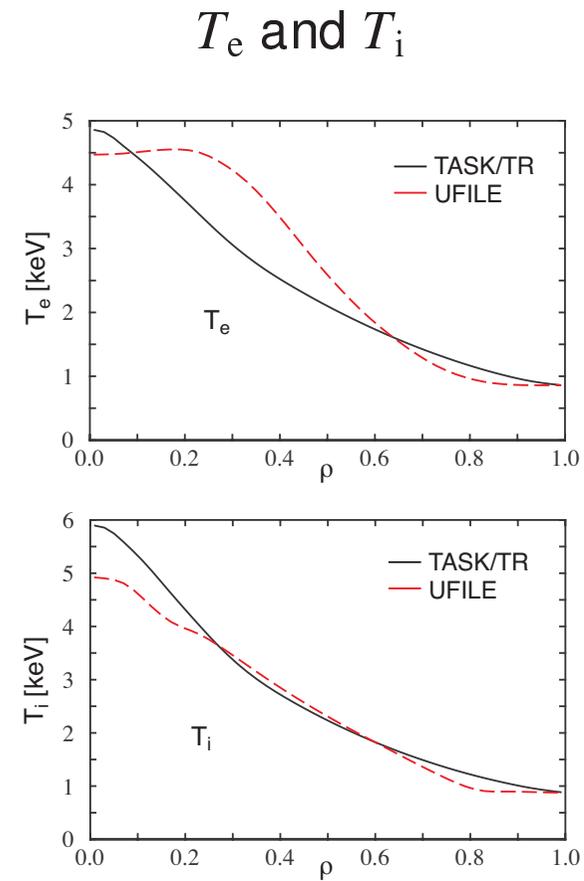
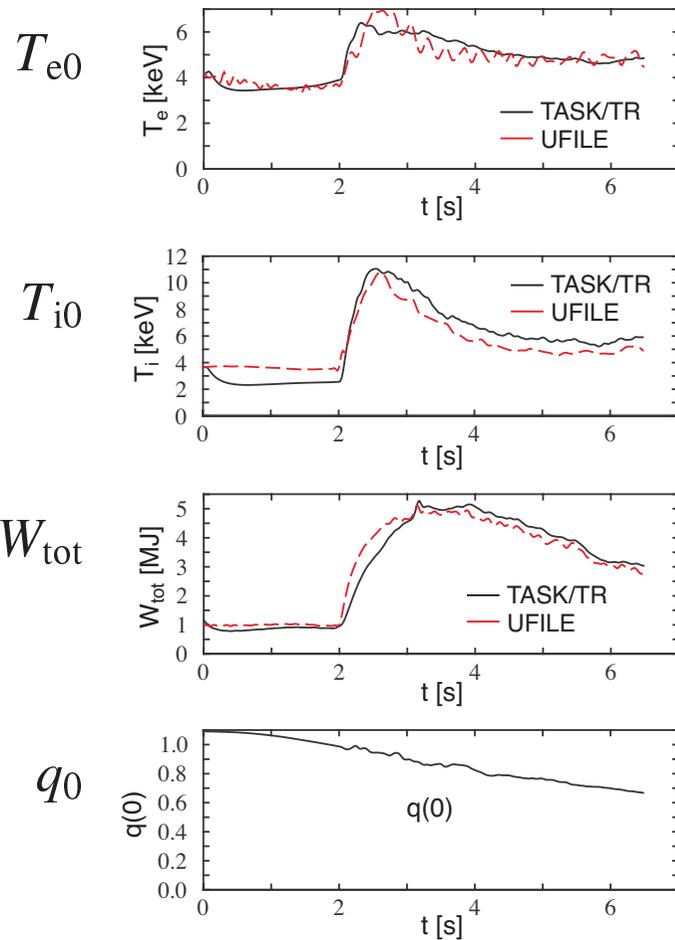
- Edge density and temperature: given

- Transport model: Sauter + CDBM(with  $E \times B$  rotation)



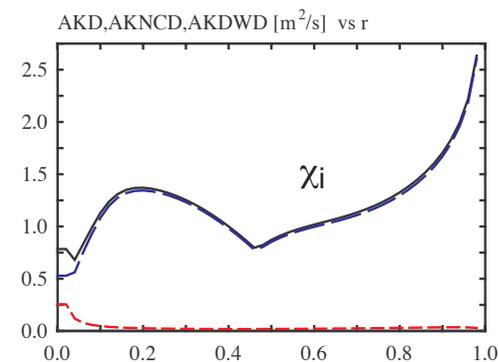
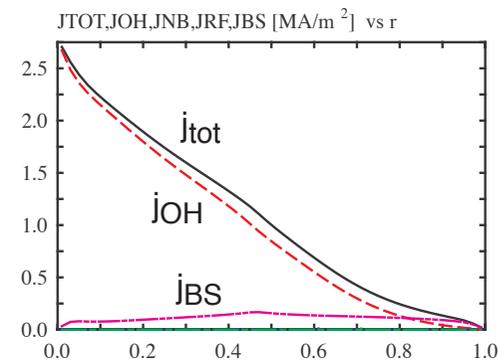
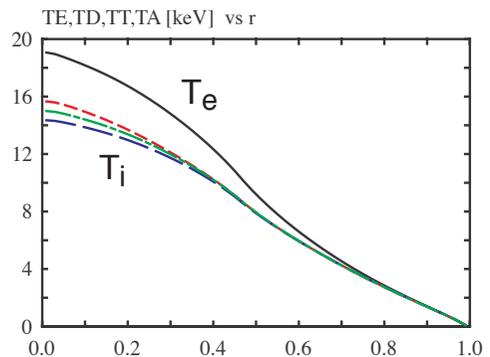
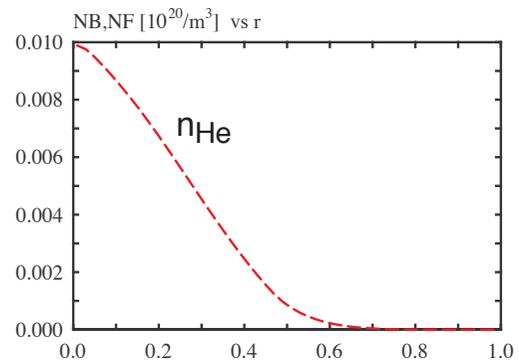
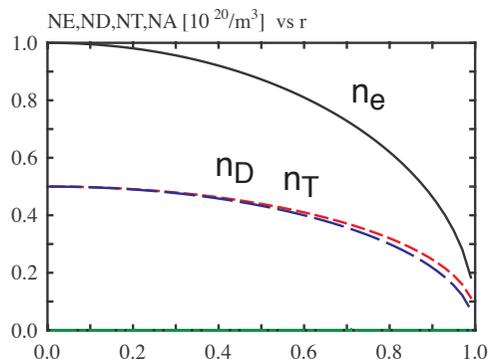
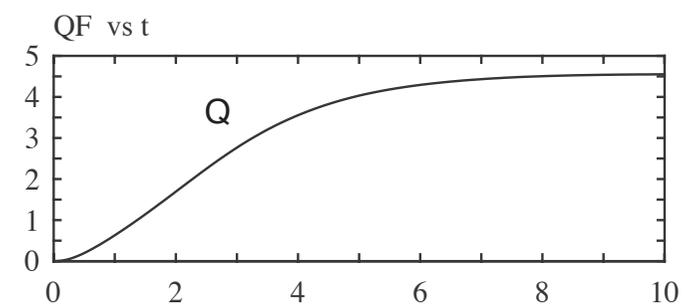
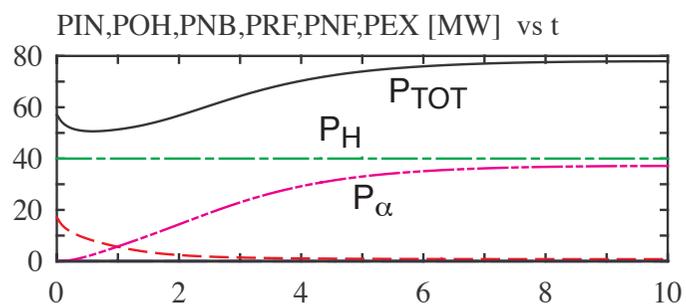
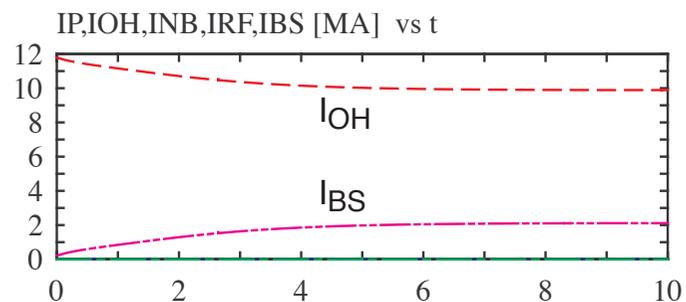
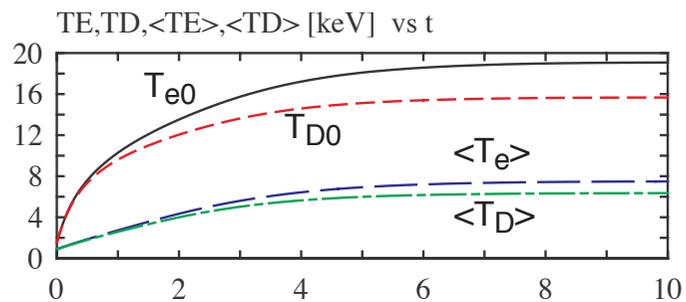
# Comparison with JET Experiment

- Shot number: 19691



- Sawtooth relaxation slightly improves  $T_e$  profile.

# Preliminary ITER simulation



# Transport Model

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- **1D Transport code (TASK/TX)** *Ref. Fukuyama et al.*
- **Two fluid equation for electrons and ions**
  - Flux surface average
  - Coupled with Maxwell equation
  - Neutral diffusion equation
- **Neoclassical transport**
  - Included as a poloidal viscosity term
  - Diffusion, resistivity, bootstrap current, Ware pinch
- **Anomalous transport**
  - Current diffusive ballooning mode
  - Ambipolar diffusion through poloidal momentum transfer
  - Perpendicular viscosity

# Dynamical Transport Equation: TASK/TX

- **Bounce-averaged transport equation** (electron, ion)

$$\frac{\partial n_s}{\partial t} = -\frac{1}{r} \frac{\partial}{\partial r} (r n_s u_{sr}) + S_s$$

$$\frac{\partial}{\partial t} (m_s n_s u_{sr}) = -\frac{1}{r} \frac{\partial}{\partial r} (r m_s n_s u_{sr}^2) + \frac{1}{r} m_s n_s u_{s\theta}^2 + e_s n_s (E_r + u_{s\theta} B_\phi - u_{s\phi} B_\theta) - \frac{\partial}{\partial r} n_s T_s$$

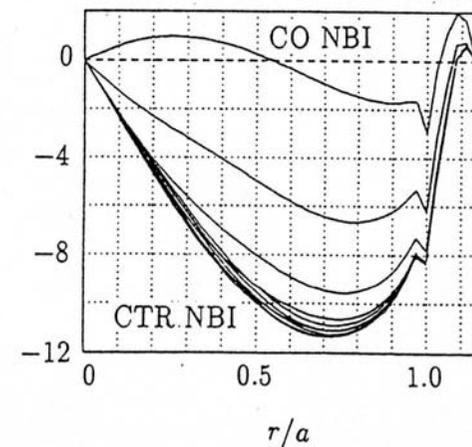
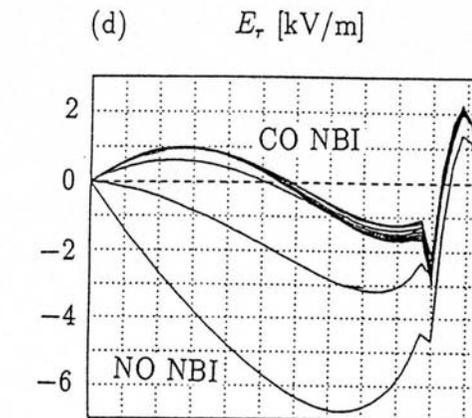
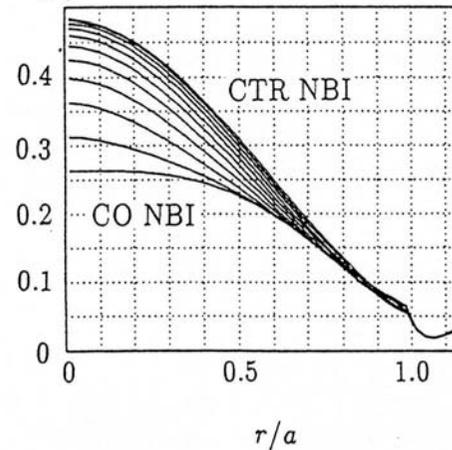
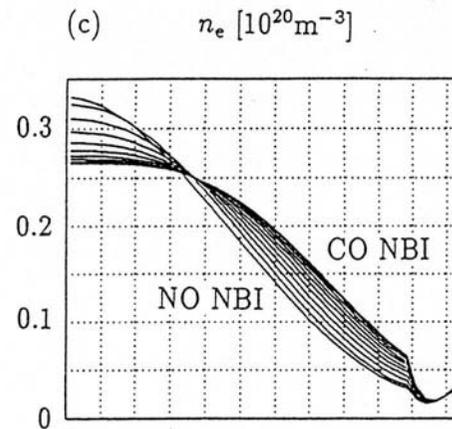
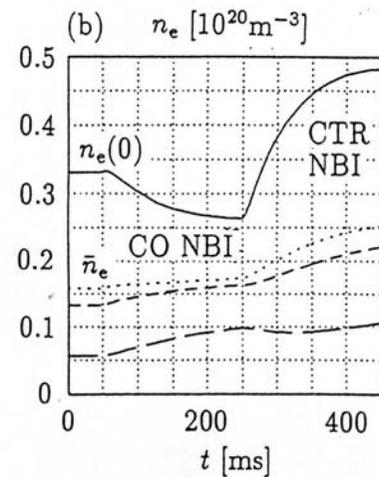
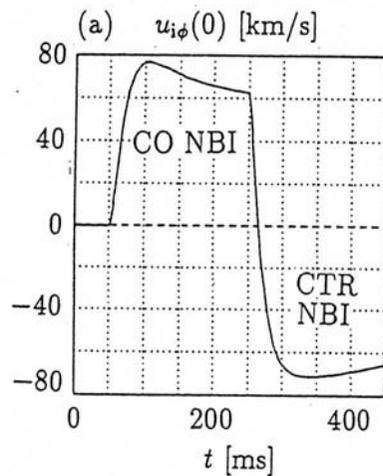
$$\begin{aligned} \frac{\partial}{\partial t} (m_s n_s u_{s\theta}) = & -\frac{1}{r^2} \frac{\partial}{\partial r} (r^2 m_s n_s u_{sr} u_{s\theta}) + e_s n_s (E_\theta - u_{sr} B_\phi) + \frac{1}{r^2} \frac{\partial}{\partial r} \left( r^3 n_s m_s \mu_s \frac{\partial}{\partial r} \frac{u_{s\theta}}{r} \right) \\ & + F_{s\theta}^{\text{NC}} + F_{s\theta}^{\text{C}} + F_{s\theta}^{\text{W}} + F_{s\theta}^{\text{X}} + F_{s\theta}^{\text{L}} \end{aligned}$$

$$\begin{aligned} \frac{\partial}{\partial t} (m_s n_s u_{s\phi}) = & -\frac{1}{r} \frac{\partial}{\partial r} (r m_s n_s u_{sr} u_{s\phi}) + e_s n_s (E_\phi + u_{sr} B_\theta) + \frac{1}{r} \frac{\partial}{\partial r} \left( r n_s m_s \mu_s \frac{\partial}{\partial r} u_{s\phi} \right) \\ & + F_{s\phi}^{\text{C}} + F_{s\phi}^{\text{W}} + F_{s\phi}^{\text{X}} + F_{s\phi}^{\text{L}} \end{aligned}$$

$$\begin{aligned} \frac{\partial}{\partial t} \frac{3}{2} n_s T_s = & -\frac{1}{r} \frac{\partial}{\partial r} r \left( \frac{5}{2} u_{sr} n_s T_s - n_s \chi_s \frac{\partial}{\partial r} T_e \right) + e_s n_s (E_\theta u_{s\theta} + E_\phi u_{s\phi}) \\ & + P_s^{\text{C}} + P_s^{\text{L}} + P_s^{\text{H}} \end{aligned}$$

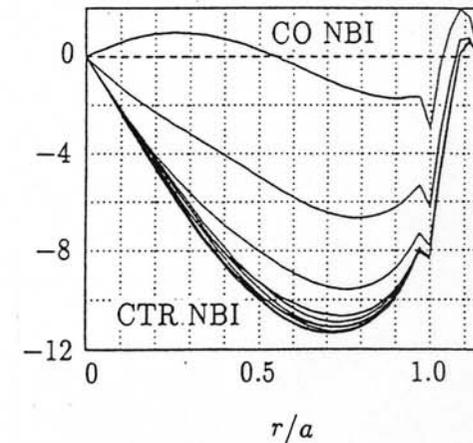
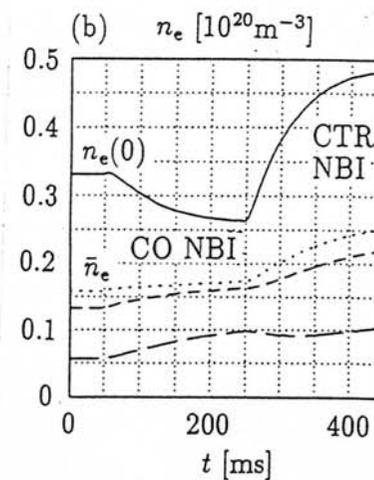
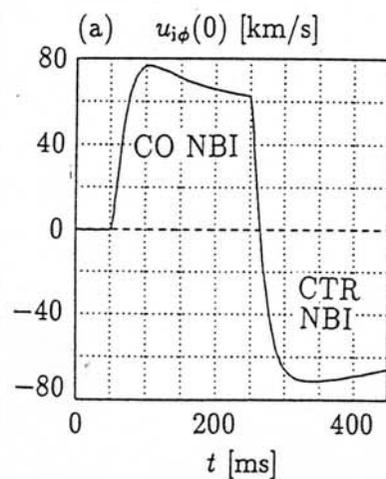
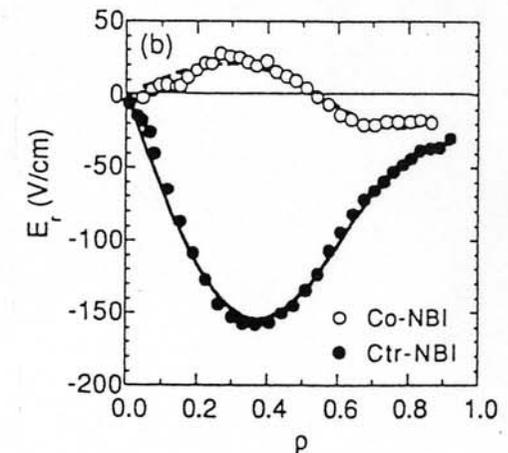
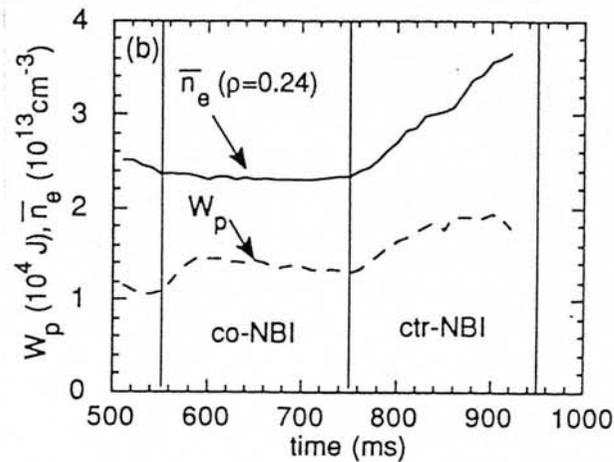
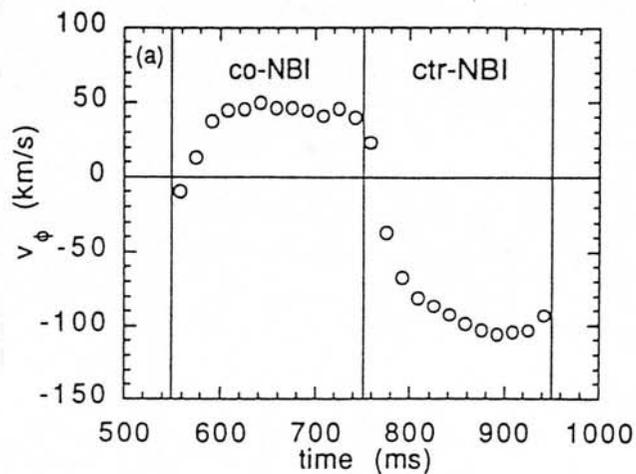
# Simulation of plasma rotation and radial electric field

- **JFT-2M parameter:** NBI co-injection  $\rightarrow$  counter-injection
- Toroidal rotation  $\Rightarrow$  Negative  $E_r$   $\Rightarrow$  Density peaking
- **TASK/TX:** Particle Diffusivity:  $0.3 \text{ m}^2/\text{s}$ , Ion viscosity:  $10 \text{ m}^2/\text{s}$



# Comparison with JFT-2M Experiment

- **JFT-2M Experiment:** Ida et al.: Phys. Rev. Lett. 68 (1992) 182
- Good agreement with experimental observation



## Summary

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- We are developing TASK code as a reference core code for burning plasma simulation based on transport analysis.
- The TASK code is composed of modules: equilibrium, transport, wave analysis, velocity space analysis, and data interface.
- Comparison of the results of TASK/TR and TASK/TX with experimental observation is ongoing for several transport models. Preliminary example of ITER burning plasma was also presented.
- **To Do**
  - Standard data interface with other simulation code
  - Systematic comparison with experimental data
  - Improvement of modules and development of new modules